

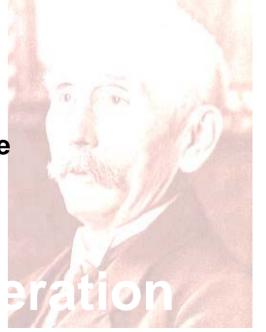


### **Carl Zeiss Industrial Metrology**

## **Algorithms**

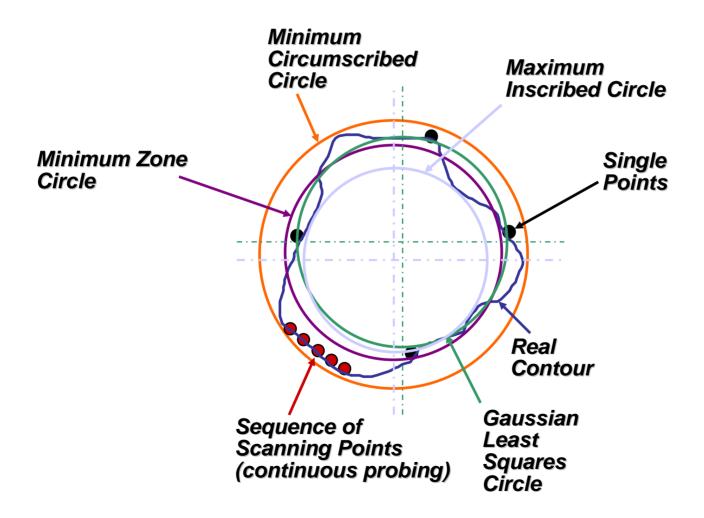
October 2005
National User Group Conference
Richard Knebel
VP Engineering – Carl Zeiss

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## Carl Zeiss IMT Algorithms

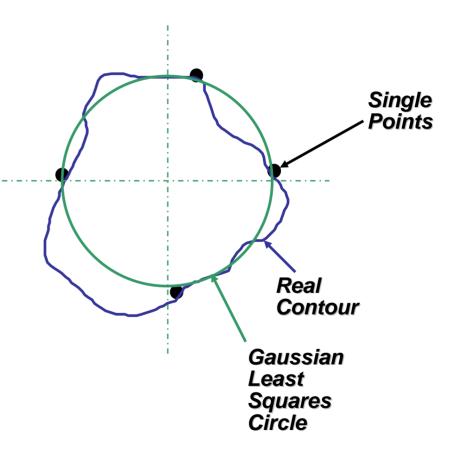




# Carl Zeiss IMT Why Least Squares?



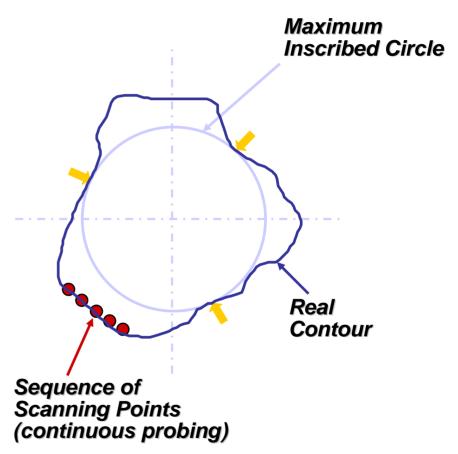
- Provides a consistent, stable result
- Consistently provides the
  - Wrong Size
  - Wrong Location
  - Wrong Form



# Carl Zeiss IMT Why Maximum Inscribed?



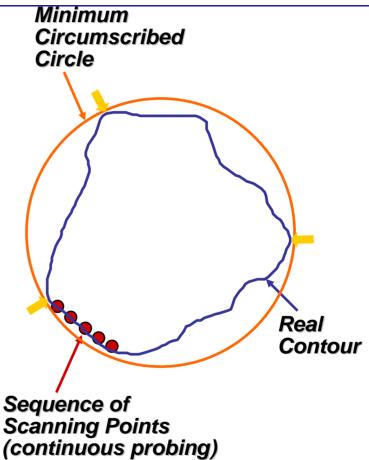
- Provides the correct result for
  - Size
  - Location
- On internal diameters
- When used with enough data density
- However it is not as stable as Least Squares because..
  - It fits on extreme points



### Carl Zeiss IMT Why Minimum Circumscribed?



- Provides the correct result for
  - Size
  - Location
- On external diameters
- When used with enough data density
- However it is not as stable as Least Squares because...
  - It fits on extreme points

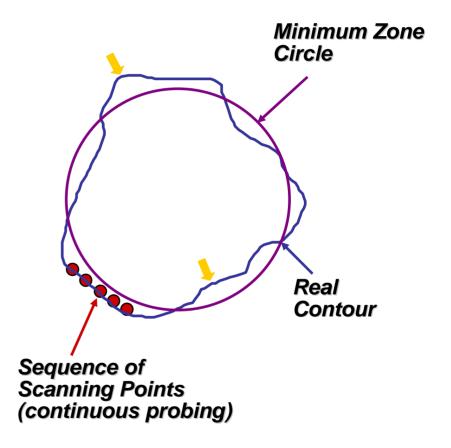


# Carl Zeiss IMT Why Minimum Zone?



- Provides the correct result for
  - Form

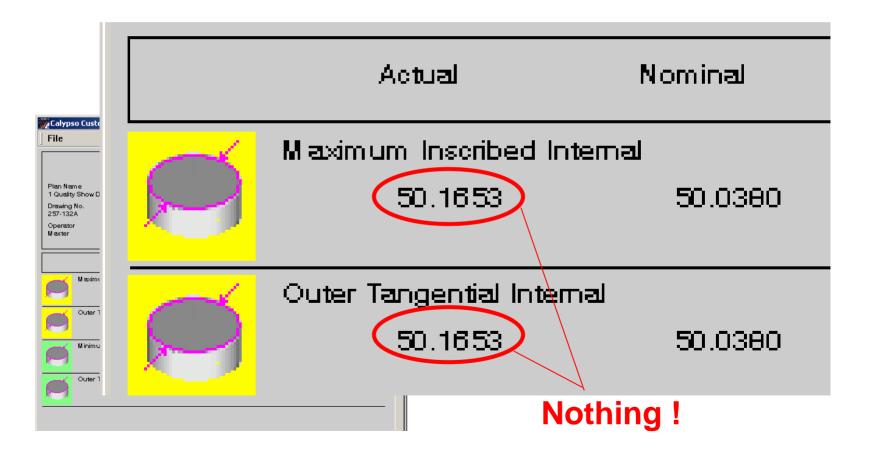
- When used with enough data density
- However it is not as stable as Least Squares because...
  - It fits on extreme points



## Carl Zeiss IMT What about Inner and Outer Tangential?



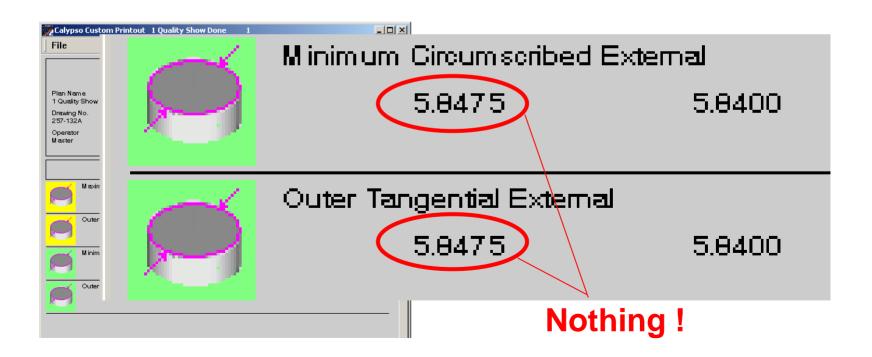
 What's the difference between Outer Tangential and Maximum Inscribed on an <u>internal</u> diameter?



# Carl Zeiss IMT What about Inner and Outer Tangential?



 What's the difference between Outer Tangential and Minimum Circumscribed on an <u>external</u> diameter?



### What about Inner and Outer Tangential?

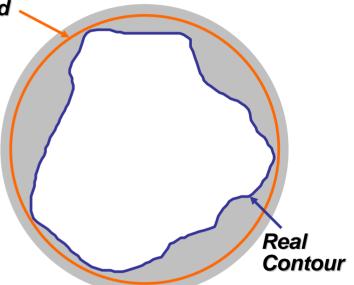


 What's the difference between Inner Tangential and Minimum Circumscribed on an <u>internal</u> diameter?

Nothing!

Minimum Circumscribed Circle

- Is this a functional mating size fit?
- No!
- When might you use it ?
- To determine if there is enough material on a casting so that it will cleanup during machining, to evaluate the maximum size, or to evaluate wall thickness

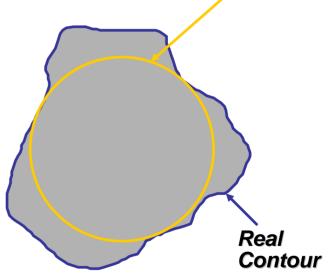


### What about Inner and Outer Tangential?



Inscribed Circle

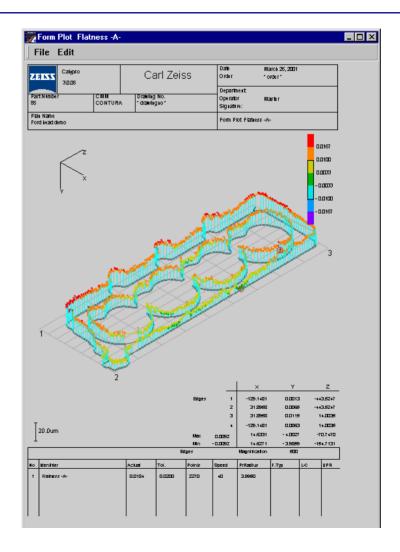
- What's the difference between Inner Tangential and Maximum Inscribed on an <u>external</u> diameter?
- Nothing!
- Is this functional mating size fit?
- No!
- When might you use it ?
- To determine if there is enough material on a casting so that it will cleanup during machining, to evaluate the minimum size, or to evaluate wall thickness



### So why do we have Inner and Outer Tangential?



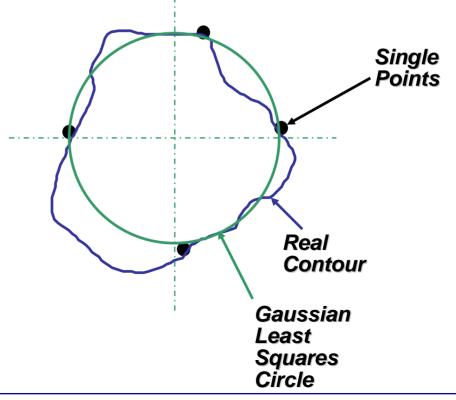
 Because it is more descriptive for Planes and Lines



## Carl Zeiss IMT So lets generalize the math



- We have Gaussian Least Squares fits which minimize the square root of the sum of the squared errors
  - In this type of fit all data points have the same weight in determining the fit
  - There is <u>absolutely nothing functional</u> about this type of fit



### Carl Zeiss IMT So lets generalize the math

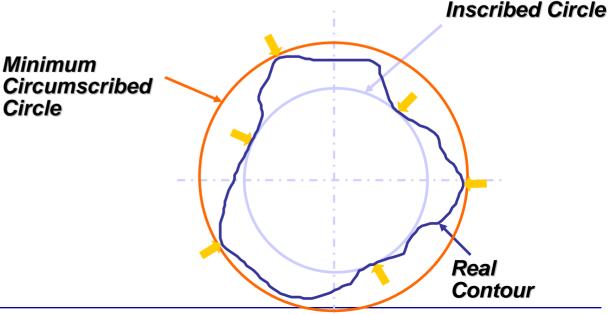


- We have <u>extrema</u> fits (Inner and Outer Tangential, Max Inscribed, Min Circumscribed) which fit on the high points of the feature
  - In this type of fit only the high points have any weight in determining the fit

This is <u>absolutely functional</u> fitting for size and location like when mating a plane against a granite surface plate, or finding the slip fit pin that just fits into a bore Maximum

**Minimum** 

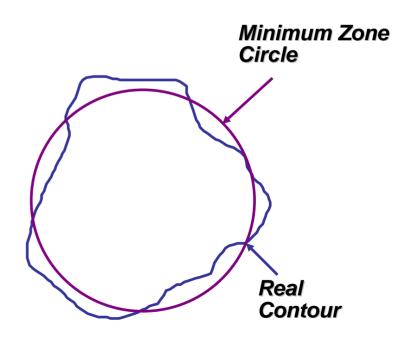
Circle



# Carl Zeiss IMT So lets generalize the math



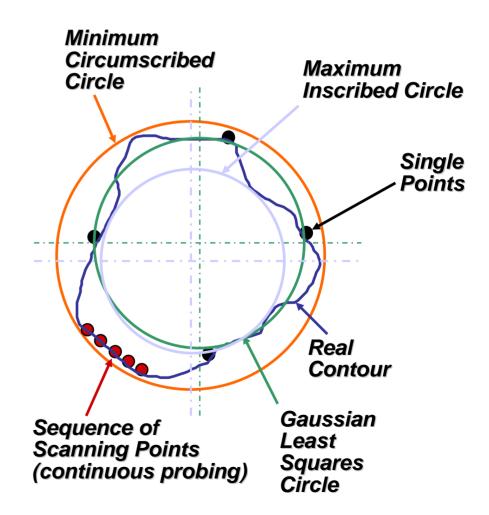
- We have <u>minimum zone</u> fits which equally balance the high and low point of the feature
  - In this type of fit only the high point and low point have any weight in determining the fit
  - This is *absolutely functional* fitting for form analysis



# Carl Zeiss IMT **Summary**



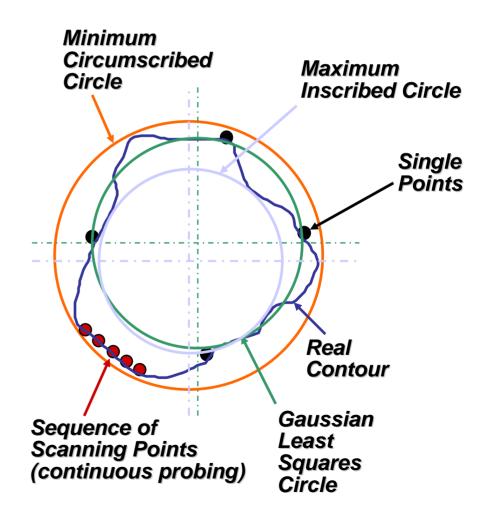
- Know the basic best math of each algorithm
- Understand the potential difference (pros and cons) each algorithm can provide
- Apply the algorithm that meets the needs of the application accordingly
- There is no one simple rule that can define what to use and when, as a CMM programmer, you must help decide what is best on a case-by-case basis



# Carl Zeiss IMT Summary



- You need to consider
  - Data density
  - Purpose of the measurement
    - Accept / Reject
    - Process control
  - Correlation concerns

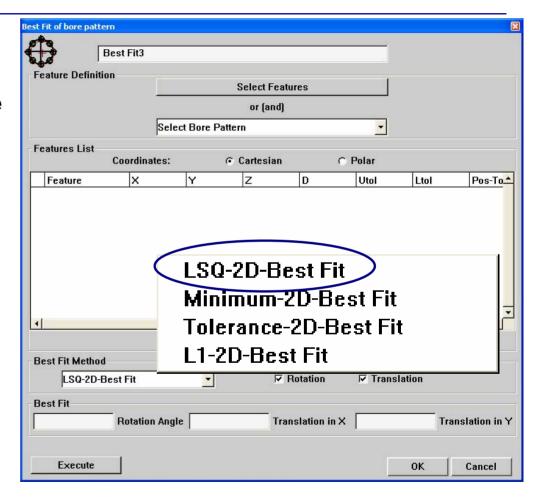


### **Bore Pattern Algorithms**



#### LSQ –2D Best Fit

- Textbook math (Gauss)
   that minimizes the square root of the sum of the squared deviations
- In certain cases it can reject a good part
- Best use is for understanding the process, not for accept/reject analysis

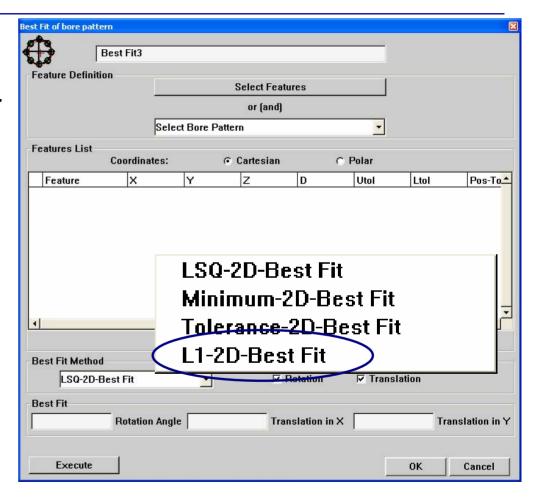


### **Bore Pattern Algorithms**



#### L1 –2D Best Fit

- Zeiss math that tries to show the worst case error more clearly
- In certain cases it can reject a good part, and will do so more than LSQ
- Best use is for understanding the process, not for accept/reject analysis, and it does this better than LSQ at showing the process problem

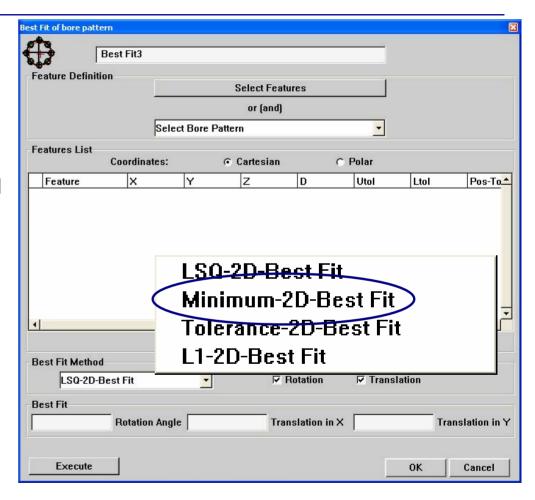


### **Bore Pattern Algorithms**



#### Minimum –2D Best Fit

- Textbook math
   (Tschebychev) that
   minimizes the maximum
   deviation
- Will at times reject a good part, but less frequently than LSQ
- Best use is for accept/reject analysis

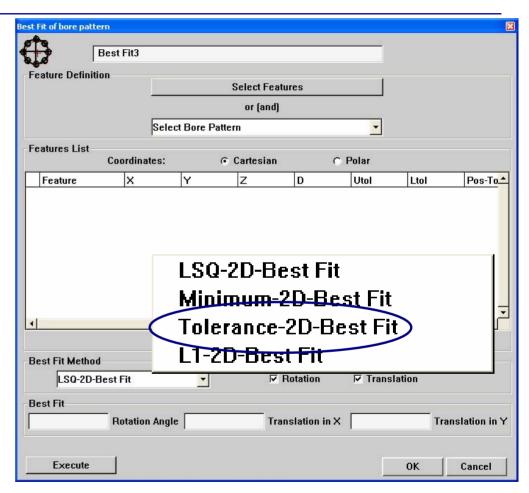


### **Bore Pattern Algorithms**



#### Tolerance –2D Best Fit

- Zeiss math that iteratively tries to accept the part like you would with a hard gage
- Will accept the maximum number of parts
- Best use is for accept/reject analysis and does a better job than Minimum







### **Carl Zeiss Industrial Metrology**

## **Questions**